General Equilibrium Theory: An Introduction by Ross M. Starr, Cambridge University Press, 1997

CORRIGENDUM¹

compiled by Jonathan Weare

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<u>Errata</u>:

Page	Line	Current Text	Correct Replacement Text
26	9 9	x y	X Y
34	18	0 [italic]	0 [roman]
37	14	(1.13)	(1.37)
51	17	of subsets of \mathbf{R}^{N}	of some subsets of \mathbf{R}^{N}
54	19	closedness of S	compactness of S
78	2		$p \neq 0$ [additional text]
85	22	Let X^h and	Let $X^h = \mathbf{R}^{\mathrm{N}}_+$ and
91	32	Note that under C.IV and CVIII, $p^{\circ} \cdot \widetilde{D}^{i}(p^{\circ}) > p^{\circ} \cdot x.$	case 1 : If $p^{\circ} \cdot \widetilde{D}^{i}(p^{\circ}) < \widetilde{M}^{i}(p^{\circ})$ then by continuity of $\widetilde{M}^{i}(\bullet)$ and $p^{\vee} \to p^{\circ}$, for \vee large we have $p^{\vee} \cdot \widetilde{D}^{i}(p^{\circ}) < \widetilde{M}^{i}(p^{\vee})$. In this case let $w^{\vee} = \widetilde{D}^{i}(p^{\circ})$. case 2 : If $p^{\circ} \cdot \widetilde{D}^{i}(p^{\circ}) = \widetilde{M}^{i}(p^{\circ})$ then by C.VIII $p^{\circ} \cdot \widetilde{D}^{i}(p^{\circ}) > p^{\circ} \cdot \hat{x}$
96	2 2	Chapter 5 Chapter 6	Chapter 4 Chapter 5

¹ It is a pleasure to thank Prof. Peter Sørensen of the University of Copenhagen. We are deeply indebted to Prof. Sørensen for his time and extensive constructive criticisms. Many of them are embodied below in the 'Errata' and 'Revised Assumptions' sections. Thanks also to Luis Pinto, Adam Sanjurjo, and Steven Sumner. Remaining errors are our own.

9'	7 10 11 17 22	1	Chapter 6 Chapter 5 and 6.2 and 6.2	Chapter 5 Chapter 4 and 4.1 and 4.1
98	8 24	ŀ	$y \in Y$	$y \in \mathbf{Y}$
1	14 17	7	$ \widetilde{\mathcal{Y}}^{0j'} $	$ \overline{\mathcal{Y}}^{\mathbf{v}j'} $
1	15 10)	$y^{v}, y^{v^{1}}, y^{v^{2}},, y^{v^{j}}$	$y^{v}, y^{v1}, y^{v2},, y^{vj},, y^{v\#F}$
12	24 17 18 19	3	we must have $D^{i}(p) \succ_{i} \widetilde{D}^{i}(p)$ $\alpha D^{i}(p) + (1 - \alpha) \widetilde{D}^{i}(p)$ $\alpha D^{i}(p) + (1 - \alpha) \widetilde{D}^{i}(p)$	there exists an $x^i \in B^i(p) \cap X^i$ with $x^i \succ_i \widetilde{D}^i(p)$ $\alpha x^i + (1 - \alpha) \widetilde{D}^i(p)$ $\alpha x^i + (1 - \alpha) \widetilde{D}^i(p)$
13	35 18	3	by theorems 8.3(b) and 9.1(b)	by theorem 8.3(b)
13	39 5		$\mathcal{Y}^{\circ i}$	$\mathcal{Y}^{\circ j}$
13	39 26	5	$M^{i}(p) = (1 - \tau)p \cdot (r^{i} - x^{i})_{+} + T,$	$M^{i}(p) = p \cdot r^{i} - \tau p \cdot (r^{i} - x^{i})_{+} + \sum_{j \in F} \alpha^{ij} p \cdot y^{j} + T, 0 < \tau < 1,$
13	39 29)	$T = (1/H)\tau \sum_{i=1}^{H} \left(p \cdot (r^{i} - x^{i})_{+} \right)$	$T = (1/\#H)\tau \sum_{i=1}^{H} \left(p \cdot (r^{i} - x^{i})_{+} \right)$
14	45 2		Assume C.IV and C.V	Assume C.I, C.II, C.IV, and CV
14	48 9,	10	nonnegative elements of $Y + \{r\}$. We will denote this set as $B = (Y + \{r\}) \cap \mathbb{R}^{\mathbb{N}}_+$, a convex set.	nonnegative elements of $Y + \{r\}$ including free disposal. We will denote this set as $B = (Y + \{r\} + \mathbb{R}^{\mathbb{N}}_{-}) \cap \mathbb{R}^{\mathbb{N}}_{+}$, a convex set, where $\mathbb{R}^{\mathbb{N}}_{-}$ is the nonpositive quadrant of $\mathbb{R}^{\mathbb{N}}$.
14	48 21		Let $B = Y + \{r\}$.	Let $B = (Y + \{r\} + \mathbf{R}^{\mathbf{N}}_{-}) \cap \mathbf{R}^{\mathbf{N}}_{+}$.
1:	50 3			$p_k = 0$ for k so that $\sum_{i \in H} x_k^{*i} < \sum_{j \in F} y_k^{*j} + r_k$. [additional text]
1:	50 3		bolds	holds

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$$M^i(p) = p \cdot \hat{r}^i - \tau p \cdot (r^i - x^i)_+ + T$$
1648 $\sum_{h \in Hq=1}^{Q} x^{h,q} = \sum_{h \in Hq=1}^{Q} r^h.$ 16410 $\frac{1}{Q} \sum_{h \in Hq=1}^{Q} x^{h,q} = \sum_{h \in H} r^h.$ 1654 $\sum_{h \in H} \bar{x}^h = \sum_{h \in H} \frac{1}{Q} \sum_{q=1}^{Q} x^{h,q} = \frac{1}{Q} \sum_{h \in Hq=1}^{Q} x^{h,q} = \sum_{h \in H} r^h.$ 16615Theorem 2.141674,5(We ignore for convenience regions where Γ^i
may coincide with a boundary derived from X^i)16715H-Q20121For functions (point-valued correspondences)
they are equivalent2116 $\min_{y \in \varphi(x)} |f^v(x) - y| < 1/v$ 2127 $\min_{y \in \varphi(x)} |f^v(x) - y| < 1/v$ 21212-16We have $f^v(x^v) = x^v...$ and we have $x^* \in \varphi(x^*)$.

$$\begin{split} M^{i}(p) &= p \cdot r^{i} - \tau p \cdot \left(r^{i} - x^{i}\right)_{+} + T \\ \sum_{h \in Hq=1}^{\sum} \sum_{q=1}^{Q} x^{h,q} &\leq \sum_{h \in Hq=1}^{Q} r^{h} \\ \frac{1}{Q} \sum_{h \in Hq=1}^{\sum} \sum_{q=1}^{Q} x^{h,q} &\leq \sum_{h \in H} r^{h} \\ \sum_{h \in H} \overline{x}^{h} &= \sum_{h \in H} \frac{1}{Q} \sum_{q=1}^{Q} x^{h,q} = \frac{1}{Q} \sum_{h \in Hq=1}^{Q} x^{h,q} \leq \sum_{h \in H} r^{h} . \end{split}$$

Theorem 14.2

(We ignore for convenience regions where Γ^i may coincide with a boundary derived from X^i . A more precise statement is that -- under C.IV, C.V -- Γ^i and Γ have non-empty interiors and $0 \notin \text{interior}(\Gamma)$)

Q-H

For functions (point-valued correspondences) into a compact range they are equivalent

 $\max_{x \in S} \min_{x^{\prime v} \in S, y^{\prime v} \in \varphi(x^{\prime v})} \left| (x, f^{v}(x)) - (x^{\prime v}, y^{\prime v}) \right| < 1/v$

 $\max_{x \in S} \min_{x^{\prime \vee} \in S, y^{\prime \vee} \in \varphi(x^{\prime \vee})} \left| (x, f^{\vee}(x)) - (x^{\prime \vee}, y^{\prime \vee}) \right| < 1/\nu$

We have $f^{\vee}(x^{\vee}) = x^{\vee}$. Recall that there is $y^{/\nu} \in \varphi(x^{/\nu})$ so that $|(x^{\vee}, f^{\vee}(x^{\vee})) - (x^{/\nu}, y^{/\nu})| < 1/\nu$. Then $x^{/\nu}, y^{/\nu} \to x^{\circ}$. But by upper hemicontinuity of $\varphi(\cdot)$, the properties $x^{/\nu} \to x^{\circ}$, $y^{/\nu} \in \varphi(x^{/\nu})$, $y^{/\nu} \to x^{\circ}$, imply $x^{\circ} \in \varphi(x^{\circ})$. Hence, choose $x^* = x^{\circ}$ and we have $x^* \in \varphi(x^*)$. QED

2142semicontinuoushemicontinuous at each $x \in \mathbf{R}$ 217Fig 17.1 $S^{y}(p^{y})$ $S^{j}(p^{y})$

221	3	$\max[ax, by]$	ax + by
225	22		$x' \in interior(X^i)$ [additional text]
226	8	But then by	Without loss of generality, let $x' \in interior(X^i)$. But then by

Note on sections 17.3-17.4: many of the results in these sections rely on our choice of boundary, *c*, and therefore require assumptions P.I-P.IV. This correction concerns Theorems 17.2-17.6, Lemmas 17.4, 17.5, 17.7, and 17.8.

<u>Revised Assumptions</u>:

The following results are valid as stated, but not all of the assumptions listed in the text are required.

- Lemma 10.1 Can delete C.V and C.VII.
- Theorem 12.1 Can delete C.V.
- Lemma 12.1 Can delete C.I, C.III, C.V, and C.VI.
- Theorem 12.2 Can delete P.II-P.IV, inasmuch as the Separating Hyperplane Theorem requires only that A and B be non-empty, convex, and disjoint.
- Corollary 12.1 Can delete P.II-P.IV.