## Answers to Exam No. 2 on Topics from Chapters 2 through 4

1..

The null hypothesis for overall significance is that the regression coefficients for HOME, INST, SVC, TV, AGE, AIR, and Y are all zero, that is, $\beta_{i}=0$ for $i=2-8$. The alternative is that at least one of them is not zero.
2..

The test statistic is given by Equation (4.4) and has the value

$$
F_{c}=\frac{(43865.001-4923.914) / 7}{4923.914 /(40-8)}=36.15
$$

3. 

Under the null hypothesis, $F_{c}$ has the $F$-distribution with d.f. 7 and 32 .
4.

The critical $F *(0.01)$ is between 3.12 and 3.30 which is less than $F_{c}$. The null hypothesis is therefore rejected.

5-7.
For individual coefficients, we carry out a $t$-test. The critical $t_{32}^{*}(0.05)$ is between 1.684 and 1.697 . If the computed $t_{c}$ is above this (numerically) we reject the null hypothesis that the corresponding regression coefficient is zero and conclude that the variable has a significant effect on the number of subscribers to cable TV. The following table gives the computed $t_{c}$ and the criterion.

|  | Coefficient | Std. Error | Test statistic | Signif./Insign. |
| :--- | :---: | :---: | :---: | :--- |
| $\hat{\beta_{1}}$ | -6.808 | 26.7 | Ignore | Ignore |
| $\hat{\beta_{2}}$ | 0.406 | 0.035 | 11.600 | Significant |
| $\hat{\beta_{3}}$ | -0.526 | 0.476 | -1.105 | Insignificant |
| $\hat{\beta_{4}}$ | 2.039 | 2.127 | 0.959 | Insignificant |
| $\hat{\beta_{5}}$ | 0.757 | 0.688 | 1.100 | Insignificant |
| $\hat{\beta_{6}}$ | 1.194 | 0.502 | 2.374 | Significant |
| $\hat{\beta_{7}}$ | -5.111 | 1.518 | -3.367 | Significant |
| $\hat{\beta_{8}}$ | 0.0017 | 0.00347 | 0.490 | Insignificant |

## 8..

The variables INST, SVC, TV, and Y are candidates to be excluded because the corresponding coefficients are not statistically significant.
9. $H_{0}: \beta_{i}=0$ for $i=3,4,5$, and 8. $H_{1}$ : At least one of them is not zero.
10. $\quad F_{c}=\frac{(5595.615-4923.914) / 4}{4923.914 /(40-8)}=1.09$
11. Under $H_{0}, F_{c}$ has the $F$-distribution with d.f. 4 and 32.
12..

For a 10 percent test, $F^{*}$ is between 2.09 and 2.14. Because $F_{c}<F^{*}$, we cannot reject the null hypothesis. Thus the omitted variables have coefficients that are jointly insignificant.

