

- a. Taking logarithms of both sides of the Cobb-Douglas production function, we get

$$\ln Q_t = \alpha + \beta \ln K_t + \gamma \ln L_t + u_t$$

- b. Let $\alpha = \alpha_1 + \alpha_2 t$, $\beta = \beta_1 + \beta_2 t$, and $\gamma = \gamma_1 + \gamma_2 t$. Substituting these in the basic model, we obtain the unrestricted model.

$$\ln Q_t = \alpha_1 + \alpha_2 t + \beta_1 \ln K_t + \beta_2 (t \ln K_t) + \gamma_1 \ln L_t + \gamma_2 \ln (t L_t) + v_t$$

- c. The variables to be generated are: $\ln Q_t$, $\ln K_t$, $\ln L_t$, $t \ln K_t$, and $t \ln L_t$.
- d. The null hypothesis is $\alpha_2 = \beta_2 = \gamma_2 = 0$. The alternative is that at least one of these coefficients is not zero.
- e. The test statistic is $F_c = \frac{(ESSR - ESSU)/3}{ESSU/(46-6)}$, where ESSR and ESSU are the error sums of squares for the restricted and unrestricted models, respectively.
- f. Under the null F_c has the F -distribution with 3 d.f. for the numerator and 40 d.f. for the denominator.
- g. The critical value is $F_{3,40}^*(0.05) = 2.84$.
- h. Reject the null hypothesis if $F_c > 2.84$.