The Cyclicality of Separation and Job Finding Rates*

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Abstract

This paper uses CPS gross flow data, adjusted for margin error and time aggregation error, to analyze the business cycle dynamics of separation and job finding rates and to quantify their contributions to overall unemployment variability. Cyclical changes in the separation rate lead those of unemployment, while the job finding rate and unemployment move contemporaneously. Fluctuations in the separation rate explain between 40 and 50 percent of fluctuations in unemployment, depending on how the data are detrended. Our results suggest an important role for the separation rate in explaining the cyclical behavior of unemployment.

JEL codes: J63, J64
Keywords: Separation rate, Job finding rate, Unemployment, CPS worker flows

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1 Introduction

The empirical behavior of U.S. job loss and hiring over the business cycle remains an elusive and controversial subject, despite decades of research. While much early work considered gross flows of workers and jobs, more recent papers have stressed the importance of transition rates faced by individual workers. Furthermore, researchers have highlighted the variability of unemployment as a key measure of aggregate labor market activity.

In this paper we assess the cyclical behavior of worker transition rates into and out of unemployment for the aggregate U.S. labor market. We focus on two specific dimensions of cyclical behavior. First, how do separation and job finding rates comove with unemployment? Second, to what extent do movements in these rates contribute to overall unemployment variability?

These questions are central to evaluating the relative roles of separation versus job finding activity in explaining unemployment movements. Higher unemployment during downturns might be triggered by higher separation rates, which generate waves of job loss. Alternatively, an initial phase of low job finding rates may drive unemployment upward. Sorting out the timing and magnitude of these channels is important for understanding the mechanisms that underlie unemployment fluctuations.

This paper addresses these issues by analyzing gross flow data from the Current Population Survey (CPS) over the 1976-2006 period. The data are adjusted for margin error in line with the approach of Abowd and Zellner (1985). We measure quarterly separation and job finding hazard rates using Shimer’s (2005a) time aggregation correction. Comovement is analyzed by considering the correlations between the two hazard rates and unemployment at various leads and lags. To quantify the contributions of separation and job finding rates, we decompose total unemployment variations into components that depend separately on each rate. We consider both HP filtering and first differencing as methods for

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2 Hall (2005b) and Shimer (2005b) stress the salience of unemployment variability as a statistic for evaluating job matching models.
3 Throughout the paper we use the terms “separation” and “job finding” to denote movements of workers out of and into employed status. Thus, we do not consider movements directly between jobs.
Our results show that cyclical changes in the separation rate tend to lead those of unemployment. In particular, the highest correlations between the separation rate and unemployment are achieved when the separation rate is lagged relative to unemployment: the correlation between the separation rate and unemployment lies above 0.5 at lags of zero to four quarters in the HP filtered data, and above 0.2 at the same lags in the first differenced data. These results show that changes in the separation rate play an important role in explaining future movements in unemployment. For the job finding rate, in contrast, the correlations are spread symmetrically about zero in both the HP filtered and first differenced data. This means that the job finding rate and unemployment tend to move contemporaneously.

To evaluate the direct comovement between the separation and job finding rates, we evaluate their cross correlations. Peaks are attained when the separation rate is lagged by one quarter, at values of roughly -0.7 and -0.4 in the HP filtered and first differenced data, respectively. Thus, much of the variability of the job finding rate can be explained by variations in the separation rate occurring in previous quarters.

To analyze the contributions of the hazard rates to unemployment variability, we follow Shimer (2005a) by approximating the unemployment rate using the theoretical steady state value associated with the contemporaneous separation and job finding rates. This allows unemployment variability to be readily decomposed by means of a conventional factor analysis. In the HP filtered data, fluctuations in the separation rate relative to trend explain 41 percent of overall fluctuations in unemployment. The figure rises to 51 percent in the first differenced data. We conclude that both job finding and separation rates are important in accounting for unemployment variability.

We also consider the contributions of the separation and job finding rates since 1985. For this subsample, we find that the separation rate explains 34 and 46 percent of unemployment fluctuations under the respective filtering methods. Thus, although the separation rate explains a smaller proportion in recent decades, its contribution remains

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4Note that it is natural for the correlations to be smaller in magnitude when the first difference filter is used.

5We also consider cross correlations between the hazard rates and GDP. We find that the separation rate leads GDP, at least weakly, while the job finding rate lags it. This is consistent with our unemployment results, since GDP tends to lead unemployment.

6Since the separation rate leads the job finding rate, this analysis may well overstate the true contribution of the job finding rate. This point is discussed further in Conclusion.
substantial.

Our findings bear on the current debate over the cyclical behavior of the separation rate. Using both gross flow- and unemployment duration-based data derived from the CPS, Shimer (2005a) argues that once time aggregation bias is taken into account, measured separation rates are nearly acyclic and play a small role in explaining unemployment fluctuations. We find, however, that the separation rate is highly countercyclical, even when we consider Shimer’s own data. We also find that, across the two Shimer data sets and two filtering methods, the separation rate explains between 28 and 56 percent of unemployment variability. Thus, the explanatory power of the separation rate is substantial by any measure.

In evaluating Shimer’s duration-based findings, Elsby et al. (2007) interpret the first differences of separation and job finding rates as a decomposition of unemployment variability. Their evidence suggests a more substantial role for separation rates than that suggested by Shimer, particularly when job loss is distinguished from labor force entry. We build on their approach by developing an exact decomposition of unemployment variability and extending the method to fluctuations in the unemployment level. Yashiv (2006a,b) carefully analyzes several existing data sources to discern the cyclical properties of U.S. gross worker flows and transition hazard rates. Among other findings, he shows that separation rates are strongly countercyclical and job finding rates are strongly procyclical when real GDP is used as the cyclical indicator. The paper proceeds as follows. Section 2 describes the data construction, Section 3 evaluates comovement, Section 4 considers the decomposition of unemployment variability, and Section 5 concludes.

2 Data

We consider measures of separation and job finding rates derived using monthly data from the Current Population Survey (CPS) for the period 1976-2006. Month-over-month transitions by individual workers between employed, unemployed and not-in-labor-force (NILF) status can be measured by matching workers that are sampled in consecutive months. Owing to sample rotation and temporary absences of individuals, transition information is unavailable for a substantial subset of the sample. This failure to match individual workers across months is referred to as margin error, and it leads to omission of possible transitions from the survey data.

The most common correction for margin error, the missing-at-random (MAR) method,
simply drops the missing observations and reweights the transitions that are measured. This procedure leads to biases, however, if types of transitions differ in their likelihood of omission. Following the important work of Abowd and Zellner (1985), we use an alternative correction that employs information on worker stocks. In particular, the MAR-based worker flow measures are reweighted in a manner that minimizes the discrepancies between officially-reported stocks of workers and the stocks that would be imputed from the flow measures. See Fujita and Ramey (2006) for details of our margin error correction.

A second problem with the data concerns the point-in-time measurement of worker status, which fails to capture transitions that are reversed within the month. To correct for this, we use the method suggested by Shimer (2005a), which links the month-over-month gross flow measures to underlying continuous-time adjustment equations. Let \( e_u t \) and \( u_e t \) denote the margin-error-adjusted gross flows from employment to unemployment and from unemployment to employment, respectively, and let \( e_{t-1} \) and \( u_{t-1} \) indicate the measured stocks of employed and unemployed workers. Then the average monthly separation and job finding rates are determined by

\[
\hat{s}_t = \frac{e_u t}{e_{t-1}}, \quad \hat{f}_t = \frac{u_e t}{u_{t-1}}. \tag{1}
\]

Assume that actual worker transitions are determined by a continuous-time process under which separation and job finding events arrive at constant rates within the month. The continuous-time separation and job finding hazard rates, denoted by \( s_t \) and \( f_t \), will satisfy

\[
\hat{s}_t = \frac{s_t(1 - e^{-(s_t+f_t)})}{s_t + f_t}, \quad \hat{f}_t = \frac{f_t(1 - e^{-(s_t+f_t)})}{s_t + f_t}. \tag{2}
\]

We use formulas (1) and (2) to compute our hazard rate series \( s_t \) and \( f_t \) from the adjusted CPS data. These monthly series are then converted to quarterly frequency by simple averaging. The resulting series cover the sample period 1976Q1-2005Q4.

For comparison purposes we consider two additional sets of measures constructed by Shimer, based on CPS gross flow and unemployment duration data, respectively. In his gross flow-based series, margin error is handled using the MAR procedure, while time aggregation error is corrected using the method discussed above. His duration-based series are adjusted for time aggregation error using a related method. See Shimer (2005a) for further details concerning his data construction.\(^7\)


\(^8\)Sample periods are 1967Q2-2004Q4 for the gross flow-based data and 1951Q1-2004Q4 for the duration-based data. The data are available at Shimer’s web page, http://robert.shimer.googlepages.com/flows.
3 Business Cycle Comovement

In this section we assess the dynamic relationships at business cycle frequencies between the separation and job finding rates $s_t$ and $f_t$ and the unemployment rate as reported by the Bureau of Labor Statistics. The dynamic relationships are measured in terms of cross-correlations at various leads and lags. We consider both HP filtering and first differencing. For the HP filter we use the standard smoothing parameter of 1600.

Results for the two detrending methods are shown in Figure 1. For HP filtered data, changes in unemployment are most highly correlated with changes in the separation rate occurring in previous quarters, i.e., the separation rate leads unemployment. The correlation with unemployment lies above 0.50 at lags of zero to four quarters in the HP filtered data, whereas the correlation between unemployment and the future separation rate reaches almost zero after four quarters. When the first difference filter is used, the magnitudes of the correlations are naturally reduced. However, one can clearly see in the upper right panel of the figure that the same dynamic pattern is preserved.

Correlations with the job finding rate, in contrast, are spread symmetrically about zero lag. This means that both future and past values of the job finding rate relate similarly to unemployment. The two variables may be viewed as moving contemporaneously.

Figure 2 repeats this exercise using GDP in place of unemployment. Under the HP filter, the separation rate leads GDP, while it is roughly contemporaneous with GDP under first differencing. The job finding rate lags GDP under either filtering method. These results are sensible since unemployment tends to lag GDP. Broadly speaking, we conclude that the separation rate moves ahead of the business cycle, while the job finding rate trails it.

Figure 3 reports the cross correlations between the separation and job finding rates under the two filtering methods. These provide a direct assessment of comovement between the two rates themselves. Observe that the HP filtered rates are strongly negatively correlated at lags of 0-4 quarters, while the first differenced rates exhibit strong negative correlation at a lag of one quarter. It follows that declines in the job finding rate tend to be preceded by increases in the separation rate. Importantly, this result suggests the possibility that some of the variability of the job finding rate is actually driven by the movements in the separation rate occurring in previous quarters.\(^9\)

\(^9\)Note that the contribution analysis in the following section does not incorporate this dynamic interaction. This issue is further discussed in Conclusion.
In Figures 4 through 6 we replicate this analysis using Shimer’s gross flow-and duration-based data sets. The results are essentially unaltered except for the first differenced duration data, where a backward phase shift in the unemployment-job finding correlations may be observed. We favor the gross flow-based findings since they are derived from direct measurements of the flows between employment and unemployment. In the duration data, these flows are confounded with flows between NILF and unemployment, leading to less reliable measures of separation and job finding rates.

4 Contributions to Unemployment Variability

We now quantify the contributions of separation and job finding rates to overall unemployment variability. Shimer (2005a) argues that the measured magnitudes of the two hazard rates make it reasonable to use the following approximation:

\[ u_t \simeq \frac{s_t}{s_t + f_t} \equiv u_t^{ss}. \]

This approximation may also be applied to the trends. Let \( \bar{u}_t \), \( \bar{s}_t \) and \( \bar{f}_t \) denoted the trend components of the three series obtained via the HP filter. We then have:

\[ \bar{u}_t \simeq \frac{\bar{s}_t}{\bar{s}_t + \bar{f}_t} \equiv \bar{u}_t^{ss}. \]

Log-linearizing \( u_t^{ss} \) around the trend values \( \bar{u}_t^{ss} \) yields the following decomposition:

\[ \ln \left( \frac{u_t^{ss}}{\bar{u}_t^{ss}} \right) = (1 - u_t^{ss}) \ln \left( \frac{s_t}{\bar{s}_t} \right) - (1 - \bar{u}_t^{ss}) \ln \left( \frac{f_t}{\bar{f}_t} \right) + \epsilon_t. \] (3)

Observe that (3) expresses the deviations of unemployment from trend as a sum of factors that depend separately on the deviations of separation and job finding rates from trend, together with a residual term.

In the case of first differencing, the trend components are given by \( u_{t-1} \), \( s_{t-1} \) and \( f_{t-1} \), and the decomposition becomes: \(^{10}\)

\[ \Delta \ln u_t^{ss} = (1 - u_{t-1}^{ss}) \Delta \ln s_t - (1 - u_{t-1}^{ss}) \ln f_t + \epsilon_t. \] (4)

Equations (3) and (4) may be expressed generically as:

\[ du_t^{ss} = du_t^{sr} + df_t^{fr} + \epsilon_t. \] (5)

\(^{10}\)This decomposition is considered in Fujita and Ramey (2007), who build on the idea put forth by Elsby et al. (2007).
Figure 7 plots the factors $du_{t}^{sr}$ and $du_{t}^{jf}$ together with the unemployment deviations $du_{t}^{ss}$ under each of the filtering methods. Under HP filtering, the factor $du_{t}^{sr}$ is somewhat less variable than $du_{t}^{jf}$, while the variabilities are comparable under first differencing. In either case, both factors display substantial variability relative to $du_{t}^{ss}$ throughout the sample period.

The linear decomposition (5) makes possible a quantitative assessment of unemployment variability in terms of the separate contributions of separation and job finding rates. Note that the variance of $du_{t}^{ss}$ may be written:

$$\text{Var}(du_{t}^{ss}) = \text{Var}(du_{t}^{sr}) + \text{Var}(du_{t}^{jf}) + \text{Var}(\epsilon_{t})$$

$$+ 2\text{Cov}(du_{t}^{sr}, du_{t}^{jf}) + 2\text{Cov}(du_{t}^{sr}, \epsilon_{t}) + 2\text{Cov}(du_{t}^{sr}, \epsilon_{t})$$

$$= \text{Cov}(du_{t}^{ss}, du_{t}^{sr}) + \text{Cov}(du_{t}^{ss}, du_{t}^{jf}) + \text{Cov}(du_{t}^{ss}, \epsilon_{t}).$$

The term $\text{Cov}(du_{t}^{ss}, du_{t}^{sr})$ gives the amount of variation in $du_{t}^{ss}$ that derives from variation in $du_{t}^{sr}$, both directly and through its correlations with $du_{t}^{jf}$ and $\epsilon_{t}$. This may be expressed as a proportion of total variation:

$$\beta^{sr} = \frac{\text{Cov}(du_{t}^{ss}, du_{t}^{sr})}{\text{Var}(du_{t}^{ss})}.$$  

Observe that $\beta^{sr}$ is formally equivalent to the concept of beta in finance. Correspondingly, the proportions of variation in $du_{t}^{ss}$ that derive from $du_{t}^{jf}$ and $\epsilon_{t}$ are given by

$$\beta^{jf} = \frac{\text{Cov}(du_{t}^{ss}, du_{t}^{jf})}{\text{Var}(du_{t}^{ss})}, \quad \beta^{f} = \frac{\text{Cov}(du_{t}^{ss}, \epsilon_{t})}{\text{Var}(du_{t}^{ss})}.$$

From (6) we have $1 = \beta^{sr} + \beta^{jf} + \beta^{f}$. Thus, the three betas serve to decompose the total variation in $du_{t}^{ss}$ into the separate components that derive from fluctuations in separation and job finding rates, together with a residual component.

Panel A of Table 1 reports the values of betas calculated under the two filtering methods. In the HP filtered data, fluctuations in the separation rate relative to trend explain 41 percent of overall fluctuations in unemployment. The figure rises to 51 percent in the first differenced data. We conclude that separation and job finding rates account for comparable proportions of unemployment variability. In particular, cyclical fluctuations in the separation rate explain between 40 and 50 percent of the fluctuations in unemployment.

Betas for the post 1985 subsample are also reported. The contribution of the separation rate falls to 34 and 46 percent under the respective filtering methods. Thus, while
the separation rate explains a smaller proportion of unemployment fluctuations in recent decades, its contribution remains substantial.

Results obtained using the Shimer data sets are reported in panel B. The proportions explained by the separation rate are somewhat greater in his gross flow-based data, which are not corrected for margin error. In his duration-based data, the proportion explained by the separation rate drops to 28 percent under HP filtering, and 40 percent under first differencing. The proportions for the post 1985 subsample lie in a range of 15 to 42 percent, with lower values associated with the duration data. Again, we favor the gross flow-based findings since they directly isolate the flows between employment and unemployment. In the duration data, these flows are confounded with flows between NILF and unemployment. As demonstrated by Elsby et al. (2007), rates of unemployment inflow from employment are more countercyclical than overall unemployment inflow rates. In any event, all three data sets show that the separation rate makes an important contribution to unemployment variability.

5 Conclusion

Drawing on CPS gross flow data, adjusted for margin error and time aggregation error, we demonstrate that cyclical changes in the separation rate tend to lead those of unemployment, while the job finding rate and unemployment move contemporaneously. Moreover, the two rates account for roughly similar proportions of overall unemployment variability. These conclusions are robust to the detrending method, and the basic pattern holds when GDP is used in place of unemployment as an indicator of the business cycle. The conclusions also hold for Shimer’s (2005a) gross flow-based data. While his duration-based data yield a somewhat smaller contribution of the separation rate when the HP filter is adopted as a detrending method (28 percent), this data set suffers from problems in identifying flows between unemployment and employment. The gross flow-based data, in contrast, provide direct measures of these flows.

We find that movements in the job finding rate tend to be preceded by movements in the separation rate. It should be noted that the steady state approximation technique used in constructing the contribution measures suppresses this dynamic interaction, and thus the measures may significantly understate the true contributions of the separation rate. For example, a high separation rate in the current quarter is likely to be followed by a low job finding rate in the following quarter. The approximation method links the low job
finding rate to high unemployment in the following quarter, even though the separation rate was the true cause.

Our results suggest that in analyzing unemployment adjustment over the business cycle, researchers should consider fluctuations at both the separation and job finding margins. The commonly made assumption of constant separation rates cannot be justified on grounds of empirical realism or quantitative relevance. Moreover, since declines in the job finding rate tend to be preceded by increases in the separation rate, abstracting from cyclical adjustment in the separation rate may distort the analysis of unemployment dynamics.

References


Eran Yashiv. U.S. labor market dynamics revisited. IZA discussion paper 2445, November 2006b.
Table 1: Contributions to Unemployment Fluctuations: betas

A. Fujita-Ramey Data

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B. Shimer data

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Notes: See text for definitions of $\beta^*$, $\beta^J$ and $\beta^c$. Full samples cover 1976Q1-2005Q4 for Fujita-Ramey data, 1967Q2-2004Q4 for Shimer gross flow-based data and 1951Q1-2004Q4 for Shimer duration-based data. Post-1985 results are based on the samples starting at 1985Q1. Fujita-Ramey series are adjusted for margin error, and all series are adjusted for time aggregation error. See Fujita and Ramey (2006) and Shimer (2005a) for data construction details.
Figure 1: Cross correlations between unemployment rate and transition hazard rates

Figure 2: Cross correlations between GDP and transition hazard rates

Figure 3: Cross correlations between job finding rate at $t$ and separation rate at $t + i$

Figure 4: Cross correlations between GDP and transition hazard rates: Shimer data

Notes: Samples covers 1967Q2-2004Q4 for Shimer gross flow-based data and 1951Q1-2004Q4 for Shimer duration-based data. Series are adjusted for time aggregation error. See Shimer (2005a) for data construction details.
Figure 5: Cross correlations between unemployment rate and transition hazard rates: Shimer data

Notes: Samples covers 1967Q2-2004Q4 for Shimer gross flow-based data and 1951Q1-2004Q4 for Shimer duration-based data. Series are adjusted for time aggregation error. See Shimer (2005a) for data construction details.
Figure 6: Cross correlations between job finding rate at $t$ and separation rate at $t + i$: Shimer data

\[
\begin{align*}
\text{HP filtered} & \\
\text{First Difference} & \\
\end{align*}
\]

Notes: Samples covers 1967Q2-2004Q4 for Shimer gross flow-based data and 1951Q1-2004Q4 for Shimer duration-based data. Series are adjusted for time aggregation error. See Shimer (2005a) for data construction details.
Figure 7: Contributions of separation and job finding rates to business cycle movements of unemployment rate

Notes: Solid lines indicate $du_t^{s}$ and $du_t^{fr}$. Dashed lines indicate $du_t^{s*}$. See text for definitions. Sample period is 1976Q1-2005Q4. Shaded areas indicate NBER-dated recessions.